

DISCUSSION OF  
“PUBLIC DEBT AS PRIVATE LIQUIDITY: OPTIMAL POLICY”  
BY  
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## SUMMARY

### This paper

- ▶ **solves** for optimal fiscal policy with distortionary taxes & debt liquidity yield
- ▶ **finds** that the gov. trades off tax smoothing/liquidity provision/interest rate manipulation

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## Discussion

1. Overview
2. Comments

# A SIMPLIFIED 2-PERIOD MODEL

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### Environment

- Households

$$\max_{c_1, c_2, a_1, n_1, n_2} c_1 - n_1^2/2 + V(a_1) + \beta (c_2 - n_2^2/2)$$

$$\text{s.t.: } c_1 + q_1 a_1 = w_1 n_1$$

$$c_2 = w_2 n_2 + a_1$$

- Firms:  $\max\{(1 - \tau_t)An_t - w_t n_t\}$
- Government:  $g = \tau_1 An_1 + q_1 b_1$ ,  $g + b_1 = \tau_2 An_2$
- Market clearing:  $c_t + g = An_t$ ,  $b_1 = a_1$

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## Solution

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- Prices:  $q_1 = \beta + V'(b_1)$
- Government revenue:  $s_t = \tau_t(1 - \tau_t)A^2$  (the Laffer curve)



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## MAIN RESULT

### Policy problem

$$\begin{aligned}U &= c_1 - n_1^2/2 + V(a_1) + \beta \left( c_2 - n_2^2/2 \right) \\&= \frac{1}{2}A^2 \left[ 1 - \tau(s_1)^2 \right] + \beta \frac{1}{2}A^2 \left[ 1 - \tau(s_2)^2 \right] + V(b_1) + t.i.p. \\&= U(s_1) \qquad \qquad \qquad + \beta U(s_2) \qquad \qquad \qquad + V(b_1) + t.i.p.\end{aligned}$$

$$\text{s.t.: } g = s_1 + b_1 [V'(b_1) + \beta],$$

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## MAIN RESULT

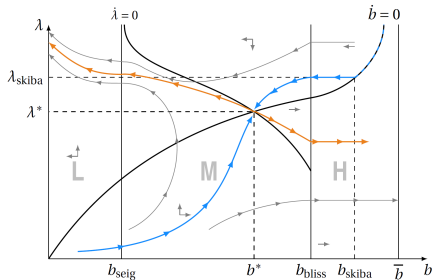
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### The main formula

$$V'(b_1) + [-U'(s_1)]V'(b_1) \left[ 1 + \frac{V''(b_1)b_1}{V'(b_1)} \right] + \beta [U'(s_2) - U'(s_1)] = 0$$

# A DYNAMIC MODEL



Steady state

$$V'(b^*) + [-U'(s^*)]V'(b^*) \left[ 1 + \frac{V''(b^*)b^*}{V'(b^*)} \right] = 0$$

$$\text{where } s^* = g + (\rho - V'(b^*))b^*.$$

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- $dV'(b)/d \log b = -0.017$  (Krishnamurthy, Vissing-Jorgensen, 2012)

$$1 + \frac{V''(b)b}{V'(b)} = 1 + \frac{1}{V'(b)} \cdot \frac{dV'(b)}{d \log b} = 1 + \frac{1}{0.035 - 0} \cdot (-0.017) > 0$$

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### Numerical value of optimal debt?

## COMMENT 2: OPEN ECONOMY

Current paper considers a closed economy.

### Foreign demand for safe assets

- Domestic safe assets are purchased by foreigners
- The benefits of liquidity creation may not all be felt at home

### Foreign supply of safe assets

- Safe interest rate may be determined by the world supply of safe assets
- Domestic debt issuance may have a limited effect on liquidity yield

Over/under supply of safe assets in the world?

## COMMENT 3: SOURCE OF $V(b)$ MATTERS

$$r(b) = \rho - V'(b)$$

### Microfoundation in the paper

- precautionary saving (Bewley, Aiyagari)
- debt as collateral (Woodford, 1990; Holmström and Tirole, 1998)

### Other sources

- Adverse selection + info-insensitive debt (Dang, Gorton, Holmstrom, 2020)
- Disasters (Kocherlakota, 2021; Mian, Straub, Sufi, 2022)

## COMMENT 3B: DISASTERS + DEFAULT

Mehrotra, Sergeyev (2021)

- An increase in the probability of disasters  $p \uparrow$
- A (potential) decline in the safe interest rate  $r_t \downarrow$
- A decline in the level of maximum sustainable debt  $\bar{b} \downarrow$

It is possible that the optimal response here is to reduce government debt

# CONCLUSION

- ▶ A very interesting, polished, and relevant paper!
  
- ▶ Comments:
  - a simple calibration
  - open economy
  - the source of low  $r$  matters + lower rates may imply lower debt